

WORKING WITH FORMULAS

* Remember that multiplication can be symbolized using parenthesis, as in $(2)(5) = 10$, the cross symbol, " \times ", as in $2 \times 5 = 10$, or the star symbol, " $*$ ", as in $2 * 5 = 10$. In addition, if two variables are simply written next to each other, we may assume that they are being multiplied.

* Note that sometimes different subscripts on the same letter are used to denote different variables, such as b_0 (pronounced "*b-naught*"), and b_1 , (pronounced "*b-one*" or "*b-sub-one*").

* You should also familiarize yourself with certain Greek letters such as μ (pronounced "*myoo*"), σ (pronounced "*sigma*"), and α (pronounced "*alpha*").

Model Problems:

In the following exercises a formula is given, along with the values of all but one of the variables in the formula. Find the value of the variable that is not given:

1. $y = mx + b; m = 3.4, x = 5.62, b = -780$

$$y = 3.4(5.62) + (-780)$$

Plug in the given values, placing any negative values in parenthesis if necessary

$$y = 19.108 - 780$$

Isolate the unknown variable if necessary

$$y = -760.892$$

Evaluate

2. $y = m * x + b; y = 1000, m = -20.5, x = 150$

$$1000 = (-20.5) * 150 + b$$

$$1000 = -3075 + b$$

$$b = 1000 + 3075$$

$$b = 4075$$

3. $y = b_1x + b_0; b_1 = 1.6, b_0 = -3, y = 100$

$$100 = 1.6x + (-3)$$

$$100 = 1.6 * x - 3$$

$$\frac{100 + 3}{1.6} = x$$

$$x = 64.375$$

4. $z = \frac{x - \mu}{\sigma}; x = 300, \mu = 250, \sigma = 40$

$$z = \frac{300 - 250}{40}$$

$$z = \frac{50}{40}$$

$$z = 1.25$$

5. $F = \left(\frac{9}{5}\right) C + 32; C = 40$

$$F = \left(\frac{9}{5}\right) 40 + 32$$

$$F = \left(\frac{360}{5}\right) + 32$$

$$F = 72 + 32 = 104$$

Practice Exercises:

In the following exercises a formula is given, along with the values of all but one of the variables in the formula. Find the value of the variable that is not given:

1. $y = mx + b; m = -12.111, x = 52.7, b = 1500$
2. $y_2 - y_1 = m(x_2 - x_1); y_2 = 6, y_1 = 3, x_1 = 2; x_2 = 4$
3. $y = b_1 * x + b_0; y = 256.5, b_1 = -30, b_0 = 101.1$
4. $z = \frac{x - \mu}{\sigma}; x = 300, \mu = 225, \sigma = 25$
5. $x = z(\sigma) + \mu; z = -1.61, \sigma = 13, \mu = 200$
6. $F = \left(\frac{9}{5}\right) C + 32; C = 85$
7. $z = \frac{x - \mu}{\sigma}; x = 550, z = 1.2, \sigma = 50$
8. $z * \sigma + \mu = x; z = -2, \mu = 10, x = 6$
9. $V = C \left(1 - \frac{n}{N}\right); n = 20, C = \$50,000, N = 5$
10. Body Mass Index: $BMI = \frac{W}{H^2} (703); w=196, H = 70$

Answers:

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|-------------------|----------------------|----------------|-----------------|
| 1. $y = 861.7503$ | 2. $m = \frac{3}{2}$ | 3. $x = -5.18$ | 4. $z = 3$ |
| 5. $x = 179.07$ | 6. $C = 185$ | 7. $\mu = 490$ | 8. $\sigma = 2$ |
| 9. $v = -150,000$ | 10. $BMI = 28.1$ | | |