

Hunter College of The City University of New York

MATH 454 Calculus on Manifolds 3 hrs, 3 cr.

Textbook: *Calculus on Manifolds* by Michael Spivak, Westview Press

Euclidean Space

- Subsets on Euclidean space
- Inner product and norms
- Functions and continuity

Differentiation

- Basic theorems
- Inverse functions
- Implicit function theorem

Integration

- Measure zero and content zero
- The Riemann integral
- Necessary and sufficient conditions for integrability
- Fubini's Theorem
- Change of variables

Integration on chains

- Algebraic preliminaries
- The tensor and exterior algebras
- Stokes' theorem for chains

Manifolds

- Fields and forms on manifolds
- Stokes' theorem on manifolds
- The volume element
- The classical integral theorems